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# STANDARD

# ISO/IEC 15946-1

Second edition 2008-04-15

# Information technology — Security techniques — Cryptographic techniques based on elliptic curves —

Part 1: **General** 

Technologies de l'information — Techniques de sécurité — Techniques cryptographiques basées sur les courbes elliptiques —

Partie 1: Généralités



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Case postale 56 • CH-1211 Geneva 20
Tel. + 41 22 749 01 11
Fax + 41 22 749 09 47
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## **Foreword**

ISO (the International Organization for Standardization) and IEC (the International Electrotechnical Commission) form the specialized system for worldwide standardization. National bodies that are members of ISO or IEC participate in the development of International Standards through technical committees established by the respective organization to deal with particular fields of technical activity. ISO and IEC technical committees collaborate in fields of mutual interest. Other international organizations, governmental and non-governmental, in liaison with ISO and IEC, also take part in the work. In the field of information technology, ISO and IEC have established a joint technical committee, ISO/IEC JTC 1.

International Standards are drafted in accordance with the rules given in the ISO/IEC Directives, Part 2.

The main task of the joint technical committee is to prepare International Standards. Draft International Standards adopted by the joint technical committee are circulated to national bodies for voting. Publication as an International Standard requires approval by at least 75 % of the national bodies casting a vote.

ISO/IEC 15946-1 was prepared by Joint Technical Committee ISO/IEC JTC 1, Information technology, Subcommittee SC 27, IT Security techniques.

This second edition cancels and replaces the first edition (ISO/IEC 15946\*1:2002), which has been technically revised.

ISO/IEC 15946 consists of the following parts, under the general title Information technology — Security techniques — Cryptographic techniques based on elliptic curves:

- Part 1: General
- Part 3: Key establishment

Elliptic curve generation will form the subject of a future Part 5.

## Introduction

One of the most interesting alternatives to the RSA and F(p) based cryptosystems that are currently available are cryptosystems based on elliptic curves defined over finite fields. The concept of an elliptic curve based public-key cryptosystem is quite simple.

- Every elliptic curve over a finite field is endowed with an addition "+" under which it forms a finite abelian group.
- The group law on elliptic curves extends in a natural way to a "discrete exponentiation" on the point group
  of the elliptic curve.
- Based on the discrete exponentiation on an elliptic curve, one can easily derive elliptic curve analogues of the well-known public-key schemes of the Diffie-Hellman and ElGamal type.

The security of such a public-key cryptosystem depends on the difficulty of determining discrete logarithms in the group of points of an elliptic curve. This problem is, with current knowledge, much harder than the factorisation of integers or the computation of discrete logarithms in a finite field. Indeed, since Miller and Koblitz independently suggested the use of elliptic curves for public-key cryptographic systems in 1985, the elliptic curve discrete logarithm problem has only been shown to be solvable in certain specific, and easily recognisable, cases. There has been no substantial progress in finding a method for solving the elliptic curve discrete logarithm problem on arbitrary elliptic curves. Thus, it is possible for elliptic curve based public-key systems to use much shorter parameters than the RSA system or the classical discrete logarithm based systems that make use of the multiplicative group of some finite field. This yields significantly shorter digital signatures and system parameters and the integers to be handled by a cryptosystem are much smaller.

This part of ISO/IEC 15946 describes the mathematical background and general techniques necessary for implementing any of the mechanisms described in other parts of ISO/IEC 15946 and other ISO/IEC standards.

It is the purpose of this part of ISO/IEC 15946 to meet the increasing interest in elliptic curve based public-key technology and describe the components that are necessary to implement secure elliptic curve cryptosystems such as key-exchange, key-transport and digital signatures.

The International Organization for Standardization (ISO) and International Electrotechnical Commission (IEC) draw attention to the fact that it is claimed that compliance with this document may involve the use of patents.

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# Information technology — Security techniques — Cryptographic techniques based on elliptic curves —

# Part 1: **General**

## 1 Scope

ISO/IEC 15946 specifies public-key cryptographic techniques based on elliptic curves. These include the establishment of keys for secret-key systems, and digital signature mechanisms.

This part of ISO/IEC 15946 describes the mathematical background and general techniques necessary for implementing any of the mechanisms described in other parts of ISO/IEC 15946 and other ISO/IEC standards.

The scope of this part of ISO/IEC 15946 is restricted to cryptographic techniques based on elliptic curves defined over finite fields of prime power order (including the special cases of prime order and characteristic two). The representation of elements of the underlying finite field when the field is not of prime order (i.e. which basis is used) is outside the scope of this part of ISO/IEC 15946.

ISO/IEC 15946 does not specify the implementation of the techniques it defines. Interoperability of products complying with this part of ISO/IEC 15946 will not be guaranteed.

