
**IT Security techniques — Encryption
algorithms —**

Part 6:
Homomorphic encryption

*Techniques de sécurité IT — Algorithmes de chiffrement —
Partie 6: Chiffrement homomorphe*





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Published in Switzerland

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Foreword

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This document was prepared by Technical Committee ISO/IEC JTC 1, *Information technology*, Subcommittee SC 27, *IT Security techniques*.

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Introduction

Homomorphic Encryption is a type of symmetric or asymmetric encryption that allows third parties (i.e. parties that are neither the encryptor nor the decryptor) to perform operations on plaintext data while keeping the data in encrypted form. The primary purpose of homomorphic encryption is to allow third parties to perform such computations on data while simultaneously ensuring that the confidentiality of the plaintext data is preserved. It is typically the case that homomorphic encryption schemes require the plaintext to be represented in the form of elements of a group, rather than strings of bits or bytes as is the case with most conventional methods of encryption.

Homomorphic encryption mechanisms can be categorized by the nature of the operation(s) on the plaintext that they can support. This document considers homomorphic encryption mechanisms where the plaintext operation is typically addition and/or multiplication in a prescribed group.

IT Security techniques — Encryption algorithms —

Part 6: Homomorphic encryption

1 Scope

This document specifies the following mechanisms for homomorphic encryption.

- Exponential ElGamal encryption;
- Paillier encryption.

For each mechanism, this document specifies the process for:

- generating parameters and the keys of the involved entities;
- encrypting data;
- decrypting encrypted data; and
- homomorphically operating on encrypted data.

[Annex A](#) defines the object identifiers assigned to the mechanisms specified in this document. [Annex B](#) provides numerical examples.

2 Normative references

There are no normative references in this document.